00 Programming

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General advice

When writing R code (or any code), there are some important rules

- 1. Write script files (which you save) and source them. Don't do everything in the console.
- 2. Don't write anything more than once. This has three corollaries:
 - a. If you are tempted to copy/paste, don't.
 - b. Don't use *magic numbers*. Define all constants at the top of the script.
 - c. Write functions.
- 3. The third is **very important**. Functions are easy to test. You give different inputs and check whether the output is as expected. This helps catch mistakes.
- 4. There are two kinds of errors: syntax and function.
 - a. The first R can find (missing close parenthesis, wrong arguments, etc.
 - b. The second you can only catch by thorough testing (see the HW)
- 5. Don't use magic numbers.
- 6. Use meaningful names. Don't do this:

```
data("ChickWeight")
out <-lm(weight ~ Time + Chick + Diet, data = ChickWeight)</pre>
```

- 7. Comment things that aren't clear from the (meaningful) names
- 8. Comment long formulas that don't immediately make sense:

Simple stuff

• Vectors: x <- c(1, 3, 4) x ## [1] 1 3 4 x[1] ## [1] 1 x[-1] ## [1] 3 4

```
• Matrices:
x <- matrix(1:25, 5, 5)
х
##
       [,1] [,2] [,3] [,4] [,5]
## [1,]
         1
              6
                  11
                       16
                            21
## [2,]
              7
          2
                  12
                       17
                            22
## [3,]
         3
              8
                  13
                       18
                            23
## [4,]
        4
             9 14
                       19
                            24
## [5,]
          5
             10 15
                       20
                            25
x[1,]
## [1] 1 6 11 16 21
x[,-1]
       [,1] [,2] [,3] [,4]
##
## [1,]
             11
       6
                  16
                       21
## [2,]
        7
              12
                  17
                       22
## [3,]
        8
              13
                  18
                       23
## [4,]
        9
              14
                  19
                       24
## [5,]
        10
              15
                  20
                       25
x[c(1,3), 2:3]
##
     [,1] [,2]
## [1,]
         6 11
## [2,]
          8
              13
```

Functions

Write lots of functions. I can't emphasize this enough.

```
f <- function(arg1, arg2, arg3=12, ...){
   stuff <- arg1*arg3
   stuff2 <- stuff + arg2
   plot(arg1, stuff2, ...)
   return(stuff2)
}
x <- rnorm(100)
y1 <- f(x, 3, 15, col=2, pch=19)</pre>
```







ora	-
- 21 (1	
ara	
	-

##	[1]	10.71208132	2.22941803	9.44295078	13.05073588	11.11064615
##	[6]	-1.25246171	15.26356015	2.01760606	2.01182887	1.68283337
##	[11]	-20.94673539	-5.08135743	8.50038217	-7.59957782	-5.39636330
##	[16]	13.52531656	-10.27707502	7.07914749	20.58977470	-0.97099630
##	[21]	-5.13934917	0.26440944	-12.87997195	-8.60207899	-0.96363040
##	[26]	-1.56036318	8.65849621	0.70898159	9.28328325	13.05031265
##	[31]	0.39576712	-4.15762751	-9.45836238	25.79867918	5.55800905
##	[36]	-4.66357908	13.90603577	-3.37672808	-6.32583264	11.19349119
##	[41]	-1.46287845	14.60427076	1.38550688	-8.74278481	-6.63695725

##	[46]	6.60212772	20.59549168	0.85449871	-14.72219828	-21.39832759
##	[51]	7.73875129	-3.44279812	13.00730822	12.89305733	-0.80006982
##	[56]	-10.42099204	0.86899886	11.41999773	10.69407115	-8.74213987
##	[61]	18.94039763	3.27611272	-6.33214008	29.68576943	6.72550056
##	[66]	6.95461681	14.47238247	0.06772114	16.48131177	-9.52881657
##	[71]	-4.68592894	11.76033209	17.15652991	-10.55936775	15.69675130
##	[76]	17.98063712	9.57343322	-7.91773765	-7.29885909	1.86444039
##	[81]	0.64614087	6.60300931	8.77161263	-7.61107150	-18.13642416
##	[86]	-14.99724479	2.85084087	15.90430650	-1.27528955	13.24650889
##	[91]	-8.47394651	8.74048336	13.20049825	-0.19821541	7.87905547
##	[96]	5.38321808	3.94856657	-3.77393745	2,53124926	17.32569980

Outputs vs. Side effects

- Side effects are things a function does, outputs can be assigned to variables
- A good example is the **hist** function
- You have probably only seen the side effect which is to plot the histogram

```
myHistogram <- hist(rnorm(1000))</pre>
```





The output

myHistogram

```
## $breaks
   [1] -4.5 -4.0 -3.5 -3.0 -2.5 -2.0 -1.5 -1.0 -0.5 0.0 0.5
                                                                       2.0
                                                                            2.5
##
                                                             1.0
                                                                 1.5
## [16]
        3.0 3.5 4.0
##
## $counts
                       19 45 100 142 183 186 156 90 48 17
##
   [1]
             0
                 0
                     6
                                                               5
                                                                   1
                                                                       1
         1
```

```
##
## $density
   [1] 0.002 0.000 0.000 0.012 0.038 0.090 0.200 0.284 0.366 0.372 0.312 0.180
##
## [13] 0.096 0.034 0.010 0.002 0.002
##
## $mids
   [1] -4.25 -3.75 -3.25 -2.75 -2.25 -1.75 -1.25 -0.75 -0.25 0.25 0.75 1.25
##
## [13] 1.75 2.25 2.75 3.25 3.75
##
## $xname
## [1] "rnorm(1000)"
##
## $equidist
## [1] TRUE
##
## attr(,"class")
## [1] "histogram"
```

Assignment

What's up with <- and =?

- These two work mostly the same but not always.
- The code <- means to assign the stuff on the right to the name on the left:

x <- 12
x; rm(x) # removing it so I can demonstrate</pre>

[1] 12

This gives x the value 12.

• Technically, this is the same as

assign('x', 12)
x; rm(x)

[1] 12

Versatility

• In that simple case = does the same thing. However, <- is more versatile. Consider:

```
median(x = 1:10)
```

```
## [1] 5.5
```

x

Error in eval(expr, envir, enclos): object 'x' not found
median(x <- 1:10)</pre>

[1] 5.5

х

[1] 1 2 3 4 5 6 7 8 9 10

General practice

• Many style guides say to **always** use <-.

• If you use <-, you should put a space on both sides. This avoids issues like

x< -3

```
## [1] FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE
```

when you meant

x <- 3

• One reason to avoid = is due to confusion with logical operators like "Does x=1?"

x=1

x==1

[1] TRUE

Flow control

```
x = 1
y = c(2,3,4,1,-1,0)
# bad if(x=1) print(x)
if (x == 1) print(x)
## [1] 1
y > x
## [1] TRUE TRUE TRUE FALSE FALSE FALSE
any(y > x)
## [1] TRUE
! x
## [1] FALSE
all(y > x)
## [1] FALSE
while (x < 4){
 print(x)
  x = x + 1
}
## [1] 1
## [1] 2
## [1] 3
for (i in 1:4) print(x + i)
## [1] 5
## [1] 6
## [1] 7
## [1] 8
ifelse(any(y > x), 'yes', 'no')
## [1] "no"
```

Some functions

```
qpareto1 <- function(p, exponent, threshold) {</pre>
 # gives the inverse cdf (quantile) of a Pareto distribution
  # takes 3 parameters, exponent and threshold are for the distribution
  # p is the probability you want
  # See https://en.wikipedia.org/wiki/Pareto_distribution
  threshold * ((1 - p) ^ (-1 / (exponent - 1))) # returns the last object
}
qpareto3 <- function(p, exponent, threshold, lower.tail=TRUE) {</pre>
  # add a *default* argument to decide whether we want the lower/upper tail
  if (!lower.tail) p <- 1 - p</pre>
 q <- qpareto1(p, exponent, threshold)</pre>
  return(q) # explicitly say want to return, this line is not required
}
qpareto1(.4, 2, 2)
## [1] 3.333333
qpareto3(.4, 2, 2)
## [1] 3.333333
qpareto3(.4, 2, 2, FALSE)
## [1] 5
qpareto3(.6, 2, 2)
## [1] 5
Traceback
qpareto4 <- function(p, exponent, threshold, lower.tail = TRUE) {</pre>
  # just like qpareto 3, but now we check that our inputs make sense
  stopifnot(p \ge 0, p \le 1, exponent \ge 1, threshold \ge 0)
  q <- qpareto3(p, exponent, threshold, lower.tail)</pre>
  return(q)
}
rpareto <- function(n, exponent, threshold) {</pre>
  # generates random numbers
  # Uses the "inverse cdf" method
  # https://en.wikipedia.org/wiki/Inverse_transform_sampling
  x \leftarrow vector(length = n)
  for (i in 1:n)
    x[i] <- qpareto4(rnorm(1), exponent, threshold) # there's an error here
  х
}
```

```
rpareto(10, 3, 1)
```

Error in qpareto4(rnorm(1), exponent, threshold): p >= 0 is not TRUE

• Try traceback in RStudio

```
Vectorizing
```

```
rpareto <- function(n, exponent, threshold) {</pre>
  x \leftarrow double(n) \# always preallocate space to fill in a loop
  for (i in 1:n)
    x[i] <- qpareto4(p=runif(1), exponent, threshold) # this one is correct</pre>
  х
}
rpareto_better <- function(n, exponent, threshold) {</pre>
  qpareto4(runif(n), exponent, threshold)
  # we don't need to loop because these operations operate on the vector
}
system.time(rpareto(1e6, 2, 1))
      user system elapsed
##
##
     4.433
            0.105
                     4.541
system.time(rpareto_better(1e6, 2, 1))
##
      user
            system elapsed
##
     0.022
             0.002
                      0.023
```

When might loops bad?

- The short answer is that R is not a compiled language.
- This means that whenever you write a loop, R has to re-read all the code within the loop each iteration
- This is muy slow.
- The only thing slower, is if you don't preallocate.
- Remember that line x <- vector(length=n)?
- Without that line, x would get built within the loop, starting with length 1, then length 2, etc.
- Preallocation is the most important issue to address when writing loops.

lapply vs. apply vs. sapply

- Many functions are **vectorized**, but not all.
- Arithmetic functions **are**

```
1 + 1
```

```
## [1] 2
c(1,2,3) + c(4,5,6)
## [1] 5 7 9
c(1,2,3) + 1
```

```
## [1] 2 3 4
```

```
• Some strange ones
```

```
min(5:1,pi)
```

[1] 1

pmin(5:1,pi)

[1] 3.141593 3.141593 3.000000 2.000000 1.000000

The apply variants

• These try to do things where simple loops would suffice.

• apply is for matrices (or arrays). If you want to apply a function along a dimension

		-		,		- /						-
(ma	at <- n	natrix	x(1:10	00,10))) #	the p	arenti	hesis	makes	s the	result	print
##		[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]	
##	[1,]	1	11	21	31	41	51	61	71	81	91	
##	[2,]	2	12	22	32	42	52	62	72	82	92	
##	[3,]	3	13	23	33	43	53	63	73	83	93	
##	[4,]	4	14	24	34	44	54	64	74	84	94	
##	[5,]	5	15	25	35	45	55	65	75	85	95	
##	[6,]	6	16	26	36	46	56	66	76	86	96	
##	[7,]	7	17	27	37	47	57	67	77	87	97	
##	[8,]	8	18	28	38	48	58	68	78	88	98	
##	[9,]	9	19	29	39	49	59	69	79	89	99	
##	[10,]	10	20	30	40	50	60	70	80	90	100	

sum(mat)

[1] 5050

apply(mat,2,sum) # "applies" the function "sum" to each column (2nd dimension)

[1] 55 155 255 355 455 555 655 755 855 955
for(i in seq_len(ncol(mat))) sum(mat[,i]) # same in a loop

lapply and sapply

```
• These work for lists
(z <- list(a = 1:5, b = matrix(rnorm(10), 2), c = 25))</pre>
## $a
## [1] 1 2 3 4 5
##
## $b
##
                [,1]
                           [,2]
                                       [,3]
                                                     [,4]
                                                                 [,5]
## [1,] -0.47967746 -1.7627927 -0.7448530 0.630098346 -0.04636297
## [2,] 0.04769127 0.1477334 -0.4167264 -0.003843378 1.39869655
##
## $c
## [1] 25
lapply(z, sum)
## $a
## [1] 15
##
## $b
## [1] -1.230036
##
## $c
## [1] 25
sapply(z, sum)
```

a b c ## 15.00000 -1.230036 25.000000

lapply craziness

What does this do?

sapply(lapply(1:10, rnorm), mean)

[1] 1.46547614 0.09959410 0.65481185 0.54377228 -0.03977113 -0.40519633
[7] 0.35780540 0.06884327 -0.24332721 -0.17741595

Linear models

Predict and Friends

- R has lots of functions for working with different sorts of predictive models.
- We should review how they work with lm, and how they generalize to other sorts of models.
- We'll use the **Mobility** data we saw earlier:

```
mob <- readRDS("../data/mobility.RDS")</pre>
```

Estimation Functions and Formulas

• To estimate a linear model in R: you use lm.

- What 1m returns is a complex object containing the estimated coefficients, the fitted values, a lot of diagnostic statistics, and a lot of information about exactly what work R did to do the estimation. We will come back to some of this later.
- The thing to focus on for now is the argument to lm in the line of code above, which tells the function exactly what model to estimate
- it specifies the model. The R jargon term for that sort of specification is that it is the formula of the model.

The data argument

- While the line of code above works, it's not very elegant, because we have to keep typing mob\$ over and over.
- More abstractly, it runs specifying which variables we want to use (and how we want to use them) together with telling R where to look up the variables. This gets annoying if we want to, say, compare estimates of the same model on two different data sets (in this example, perhaps from different years).
- The solution is to separate the formula from the data source:

mob.lm2 <- lm(Mobility ~ Population + Seg_racial + Commute + Income + Gini, data=mob)</pre>

- The data argument tells 1m to look up variable names appearing in the formula (the first argument) in a dataframe called mob.
- It therefore works even if there aren't variables in our workspace called Mobility, Population, etc., those just have to be column names in mob.

• In addition to being easier to write, read and re-use than our first effort, this format works better when we use the model for prediction, as explained below.

Transformations

```
mob.lm3 <- lm(
   Mobility ~ log(Population) + Seg_racial + Commute + Income + Gini,
   data = mob
)</pre>
```

- Formulas are so important that R knows about them as a special data type.
- They *look* like ordinary strings, but they *act* differently, so there are special functions for converting strings (or potentially other things) to formulas, and for manipulating them.
- For instance, if we want to keep around the formula with log-transformed population, we can do as follows:

```
form.logpop <- "Mobility ~ log(Population) + Seg_racial + Commute + Income + Gini"
form.logpop <- as.formula(form.logpop)
mob.lm4 <- lm(form.logpop, data = mob)</pre>
```

Why formulas?

- Being able to turn strings into formulas is very convenient if we want to try out a bunch of different model specifications, because R has lots of tools for building strings according to regular patterns, and then we can turn all those into formulas.
- If we have already estimated a model and want the formula it used as the specification, we can extract that with the formula function:

formula(mob.lm3)

```
## Mobility ~ log(Population) + Seg_racial + Commute + Income +
## Gini
formula(mob.lm3) == form.logpop
```

[1] TRUE

Extracting Coefficients, Confidence Intervals, Fitted Values, Residuals, etc.

If we want the coefficients of a model we've estimated, we can get that with the coefficients function:

```
coefficients(mob.lm3)
```

```
##
       (Intercept) log(Population)
                                                              Commute
                                                                                Income
                                          Seg_racial
##
      8.338558e-02
                      -2.894236e-03
                                       -5.656590e-02
                                                         1.450771e-01
                                                                          1.772105e-06
##
              Gini
     -1.621921e-01
##
mob.lm3$coefficients
                                                                                Income
##
       (Intercept) log(Population)
                                          Seg_racial
                                                              Commute
                      -2.894236e-03
                                                                          1.772105e-06
##
      8.338558e-02
                                       -5.656590e-02
                                                         1.450771e-01
##
              Gini
##
     -1.621921e-01
```

Or even

```
summary(mob.lm3)$coef
```

##		Estimate	Std. Error	t value	Pr(> t)
##	(Intercept)	8.338558e-02	2.870373e-02	2.905044	3.784114e-03
##	log(Population)	-2.894236e-03	1.874746e-03	-1.543802	1.230739e-01
##	Seg_racial	-5.656590e-02	1.713493e-02	-3.301203	1.009994e-03
##	Commute	1.450771e-01	1.934259e-02	7.500397	1.869467e-13
##	Income	1.772105e-06	2.878660e-07	6.156006	1.236337e-09
##	Gini	-1.621921e-01	2.225561e-02	-7.287695	8.277813e-13

Confidence Intervals

• If we want confidence intervals for the coefficients, we can use confint:

```
confint(mob.lm3, level = 0.90) # default confidence level is 0.95
```

##		5 %	95 %
##	(Intercept)	0.036111577	1.306596e-01
##	log(Population)	-0.005981875	1.934023e-04
##	Seg_racial	-0.084786513	-2.834528e-02
##	Commute	0.113220542	1.769336e-01
##	Income	0.000001298	2.246209e-06
##	Gini	-0.198846318	-1.255379e-01

Warning!!

• This calculates confidence intervals assuming independent, constant-variance Gaussian noise everywhere, etc., etc., so it's not to be taken too seriously unless you've checked those assumptions somehow;

Fitted values and residuals

For every data point in the original data set, we have both a fitted value (\hat{y}) and a residual $(y - \hat{y})$. These are vectors, and can be extracted with the **fitted** and **residuals** functions:

```
head(fitted(mob.lm2)) # head() gives the first few elements
##
            1
                       2
                                  3
                                              4
                                                         5
                                                                     6
## 0.07048490 0.06299687 0.06926223 0.04927934 0.05791660 0.06455628
tail(residuals(mob.lm2)) # tail() gives the last few elements
##
            736
                         737
                                       738
                                                    739
                                                                 740
                                                                               741
## -0.045252255 -0.031707484 0.004026805 0.015472295 -0.025058476 0.007091485
```

Using bits of the lm output

- You may be more used to accessing all these things as parts of the estimated model writing something like mob.lm2\$coefficients to get the coefficients.
- This is fine as far as it goes, but we will work with many different sorts of statistical models in this course, and those internal names can change from model to model.
- If the people implementing the models did their job, however, functions like fitted, residuals, coefficients and confint will all, to the extent they apply, work, and work in the same way.

```
names(mob.lm2)
```

```
## [1] "coefficients" "residuals" "effects" "rank"
## [5] "fitted.values" "assign" "qr" "df.residual"
## [9] "na.action" "xlevels" "call" "terms"
## [13] "model"
```

Methods and Classes (R-Geeky But Important)

- In R things like residuals or coefficients are a special kind of function, called **methods**. (in **python**, these are like **obj.residuals**. The dot after the object accesses methods defined for that type of object.)
- Other methods, which you've used a lot without perhaps realizing it, are plot, print and summary.
- These are a sort of generic or meta-function, which looks up the class of model being used, and then calls a specialized function which how to work with that class.
- The convention is that the specialized function is named *method.class*, e.g., summary.lm.
- If no specialized function is defined, R will try to use *method*.default.

Wherefore methods?

- The advantage of methods is that you, as a user, don't have to learn a totally new syntax to get the coefficients or residuals of every new model class
- you just use **residuals(mdl)** whether **mdl** comes from a linear regression which could have been done two centuries ago, or is a Batrachian Emphasis Machine which won't be invented for another five years.
- (It also means that core parts of R don't have to be re-written every time someone comes up with a new model class.)
- The one draw-back is that the help pages for the generic methods tend to be pretty vague, and you may have to look at the help for the class-specific functions
- Compare ?summary with ?summary.lm.

(If you are not sure what the class of your model, mdl, is called, use class(mdl).)

Making Predictions

• The point of a regression model is to do prediction, and the method for doing so is, naturally enough, called predict. It works like so:

predict(object, newdata)

- Here object is an already estimated model, and newdata is a data frame containing the new cases, real or imaginary, for which we want to make predictions.
- The output is (generally) a vector, with a predicted value for each row of newdata.
- If the rows of **newdata** have names, those will be carried along as names in the output vector.

predict(mob.lm2, newdata = mob[which(mob\$State == "AL"),])

##	89	90	91	136	140	147	151
##	0.06302814	0.05804528	0.06325527	0.07346574	0.04584468	0.06507174	0.06884769
##	152	153	154	156	157	158	159
##	0.01799403	0.03773926	0.05232423	0.03188207	0.06476723	0.03254932	0.06408194

```
library(tidyverse)
predict(mob.lm2, newdata = filter(mob, State == "AL"))
```

2 3 4 5 6 7 ## 1 ## 0.06302814 0.05804528 0.06325527 0.07346574 0.04584468 0.06507174 0.06884769 ## 8 9 10 11 12 13 14 ## 0.01799403 0.03773926 0.05232423 0.03188207 0.06476723 0.03254932 0.06408194

Remember

- It is important to remember that making a prediction does *not* mean "changing the data and reestimating the model";
- It means taking the unchanged estimate of the model, and putting in new values for the covariates or independent variables.
- (In terms of the linear model, we change x, not $\widehat{\beta}$.)
- Notice that I used mob.lm2 here, rather than the mathematically-equivalent mob.lm1.
- Because I specified mob.lm2 with a formula that just referred to column names, predict looks up columns with those names in newdata, puts them into the function estimated in mob.lm2, and calculates the predictions.
- Had I tried to use mob.lm1, it would have completely ignored newdata.
- This is one crucial reason why it is best to use clean formulas and a data argument when estimating the model.

Transformations

- If the formula specifies transformations, those will also be done on newdata;
- we don't have to do the transformations ourselves:

```
predict(mob.lm3, newdata = filter(mob, State=="AL"))
```

##	1	2	3	4	5	6	7
##	0.06907028	0.06256967	0.06773328	0.07560851	0.05136922	0.06848649	0.07059916
##	8	9	10	11	12	13	14
##	0.02782420	0.04427768	0.05771762	0.03861002	0.06773935	0.04120510	0.06764966

• The newdata does not have to be a subset of the original data used for estimation, or related to it in any way at all

Fun with predict

• It just has to have columns whose names match those in the right-hand side of the formula.

```
predict(
  mob.lm3,
  newdata = data.frame(
    Population=1.5e6, Seg_racial=0, Commute=0.5,
    Income=3e4, Gini = median(mob$Gini)
  )
)
### 1
## 0.1033759
```

```
predict(
  mob.lm3,
  newdata = data.frame(
    Population=1.5e6, Seg_racial=0,
    Commute=0.5, Income = quantile(mob$Income, c(0.05,0.5,0.95)),
    Gini=quantile(mob$Gini,c(0.05,0.5,0.95))
)
)
```

```
## 5% 50% 95%
## 0.1122663 0.1075794 0.1024651
```

Problems w/ predict

- A very common programming error is to run **predict** and get out a vector whose length equals the number of rows in the original estimation data
- and which doesn't change no matter what you do to newdata.
- This is because if **newdata** is missing, or if R cannot find all the variables it needs in it, the default is the predictions of the model on the original data.
- An even more annoying form of this error consists of forgetting that the argument is called newdata and not data:

```
head(predict(mob.lm3)) # Equivalent to head(fitted(mob.lm3))
```

```
## 1 2 3 4 5 6
## 0.06707724 0.06499898 0.06773945 0.05266410 0.06632751 0.07133333
```

More problems

- # Don't do this!
 - Returning the original fitted values when newdata is missing or messed up is not what I would have chosen, but nobody asked me.
 - Because predict is a method, the generic help file is fairly vague, and many options are only discussed on the help pages for the class-specific functions
 - compare ?predict with ?predict.lm.
 - Common options include giving standard errors for predictions (as well point forecasts), and giving various sorts of intervals.

Using Different Model Classes

• All of this carries over to different model classes, at least if they've been well-designed.

• For instance, suppose we want to estimate a kernel regression on the same data, using the same variables.

```
library(np)
mob.npbw <- npregbw(formula=formula(mob.lm2), data=mob, tol=1e-2, ftol=1e-2)
mob.np <- npreg(mob.npbw, data=mob)</pre>
```

(no need to know what all these arguments mean at the moment.)

Why this is easy

- We can re-use the formula, because it's just saying what the input and target variables of the regression are, and we want that to stay the same.
- More importantly, both 1m and npreg use the same mechanism, of separating the formula specifying the model from the data set containing the actual values of the variables.
- Of course, some models have variations in allowable formulas
 - interactions make sense for lm but not for npreg,
 - the latter has a special way of dealing with ordered categorical variables that $\verb"lm"$ doesn't
 - etc.
- After estimating the model, we can do most of the same things to it that we could do to a linear model.

We can look at a summary:

summary(mob.np)

head(fitted(mob.np))

```
##
## Regression Data: 729 training points, in 5 variable(s)
##
## No. Complete Observations: 729
## No. Incomplete (NA) Observations: 12
## Observations omitted or excluded: 374 376 386 410 440 459 485 542 613 616 637 652
##
                 Population Seg_racial
                                          Commute
                                                    Income
                                                                Gini
## Bandwidth(s):
                    1649603 0.1624437 0.03871639 2382.342 0.0318117
##
## Kernel Regression Estimator: Local-Constant
## Bandwidth Type: Fixed
## Residual standard error: 0.0302321
## R-squared: 0.6733646
##
## Continuous Kernel Type: Second-Order Gaussian
## No. Continuous Explanatory Vars.: 5
```

We can look at fitted values and residuals:

[1] 0.06430449 0.06742469 0.07513909 0.05630422 0.06187851 0.06751230
tail(residuals(mob.np))

```
## 736 737 738 739 740
## -4.472859e-02 -3.445805e-02 -6.568906e-08 2.774485e-02 -7.634712e-03
## 741
## 1.801038e-02
```

We can make predictions:

[1] 0.09849096

and we can plot things

```
par(mar=c(5,5,1,1),cex.lab=3,cex.axis=2,lwd=2,col=4,bty='n')
plot(mob.np,plot.errors.method='bootstrap')
```

